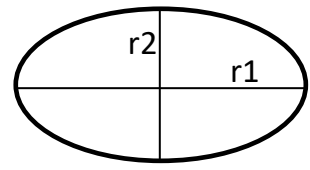


**Ellipse Algorithm:**

Ellipse is defined by center (x1, y1), first radius (r1) and second radius (r2). To draw ellipse, we must:



1. Find initial point:

$$x = x1 + r1$$

$$y = y1$$

2. Find the increment value:

$$x = x1 + r1 * \cos(\Theta) \dots\dots\dots(1)$$

$$y = y1 + r2 * \sin(\Theta)$$

by find the differential of equations (1)

$$dx = -r1 * \sin(\Theta) * d(\Theta) \dots\dots\dots(2)$$

$$dy = r2 * \cos(\Theta) * d(\Theta)$$

and from equation (1)

$$\cos(\Theta) = (x - x1) / r1 \dots\dots\dots(3)$$

$$\sin(\Theta) = (y - y1) / r2$$

substitute equation (3) in (2)

$$dx = -r1 * (y - y1) / r2 * d(\Theta) \rightarrow dx = -r1/r2 * (y - y1) * d(\Theta)$$

$$dy = r2 * (x - x1) / r1 * d(\Theta) \rightarrow dy = r2/r1 * (x - x1) * d(\Theta)$$

where  $d(\Theta) = 1 / \max(r1, r2)$

3. The iterations (number of points) are depend on angle rotation from 0 to 360.

**Ellipse Algorithm: center (x1, y1), first radius (r1), second radius (r2)**

**Begin**

$$x = x1 + r1$$

$$y = y1$$

$$\text{theta} = 0$$

$$d\text{theta} = 1 / \max(r1, r2)$$

while theta < 360

SetPixel (x, y, color)

$$x = x - (r1 / r2) * (y - y1) * d\text{theta}$$

$$y = y + (r2 / r1) * (x - x1) * d\text{theta}$$

$$\text{theta} = \text{theta} + d\text{theta}$$

End while

**End**

**Arc Algorithm**

Arc is define by center (x1, y1) , radius (r), start angle (Θ) and endangle (β). To draw Arc we must:

1. Find initial point:

$$x = x1 + r * \cos(\Theta) \dots\dots\dots(1)$$

$$y = y1 + r * \sin (\Theta)$$

2. Find the incremental value by find the differential of equations (1) :

$$dx = -r * \sin (\Theta) *d(\Theta) \dots\dots\dots(2)$$

$$dy = r * \cos (\Theta) * d(\Theta)$$

and from equation (1)

$$\cos (\Theta) = ( x - x1) / r \dots\dots\dots(3)$$

$$\sin (\Theta) = ( y - y1) / r$$

substitute equation (3) in (2)

$$dx = - ( y - y1) *d(\Theta) \rightarrow dx = ( y1 - y) *d(\Theta)$$

$$dy = ( x - x1) * d(\Theta)$$

$$\text{where } d(\Theta) = 1 / r$$

3. The iterations ( number of points) are begin from startangle(Θ) to endangle(β).

**Arc Algorithm: center (x1 , y1) , radius (r),startangle(Θ), endangle(β)**

**Begin**

$$\Theta = \text{startangle} * 3.14 / 180$$

$$\beta = \text{endangle} * 3.14 / 180$$

$$d\theta = 1 / r$$

$$x = x1 + r * \cos (\Theta)$$

$$y = y1 + r * \sin (\Theta)$$

SetPixel(x , y , color)

While Θ < β

$$x = x + ( y1 - y) *d(\Theta)$$

$$y = y + ( x - x1) * d(\Theta)$$

SetPixel(x , y , color)

$$\Theta = \Theta + d(\Theta)$$

End while

**End**